

Previous Paper Questions

1. Q.Id: 159542
 In a ΔABC , let $a, b, c, s, r, R, I, S, r_1, r_2, r_3$ stand for their usual meaning. Then match the items of List - I with those of the items of List - II

List1

List2

A. $\tan \frac{A}{2} = \frac{r}{s-a}$

I. $AI \left(\sqrt{\frac{(s-b)(s-c)}{bc}} \right)$

B. r

II. R^2

C. $(SI)^2 + 2Rr$

III.

D. $r_1^2 + r_2^2 + r_3^2$

$(4R+r+\sqrt{2}s)(4R+r-\sqrt{2}s)$

E. .

IV. $\frac{Rr}{S}$

V. $\frac{(s-b)(s-c)}{\Delta}$

A) A \rightarrow I, B \rightarrow V, C \rightarrow IV, D \rightarrow III

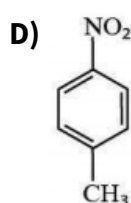
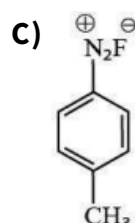
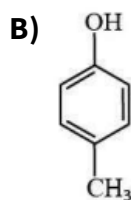
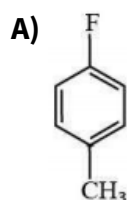
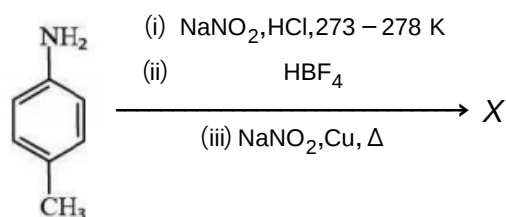
B) A \rightarrow V, B \rightarrow I, C \rightarrow II, D \rightarrow III

C) A \rightarrow V, B \rightarrow I, C \rightarrow IV, D \rightarrow III

D) A \rightarrow I, B \rightarrow IV, C \rightarrow III, D \rightarrow II

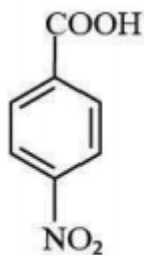
2. Q.Id: 155310

Identify X in the following.

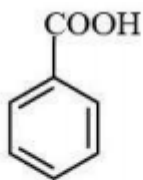


3. Q.Id: 155309

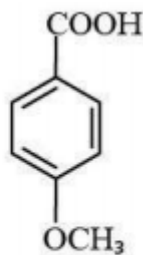
Identify the correct decreasing order of acidic strength.



(i)



(ii)



(iii)

A) (iii) > (ii) > (i)

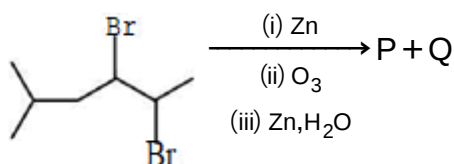
B) (i) > (ii) > (iii)

C) (ii) > (iii) > (i)

D) (i) > (iii) > (ii)

4. Q.Id: 155308

The major products P and Q in the following reaction sequences are



A) P Q

3-Methylpentanol Ethanol

B) P Q

3-Methylpentanal Ethanal

C) P Q

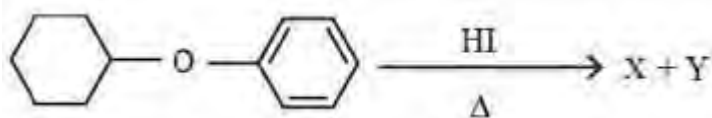
3-Methylbutanol Ethanol

D) P Q

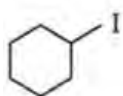
3-Methylbutanal Ethanal

5. Q.Id: 155307

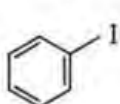
What are X and Y in the following reaction?



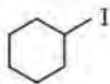
A) X



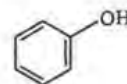
Y



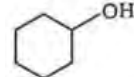
B) X



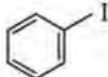
Y



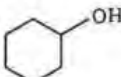
C) X



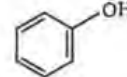
Y



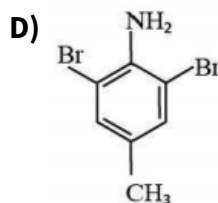
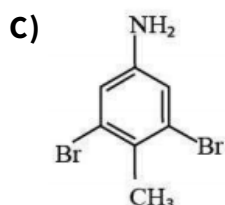
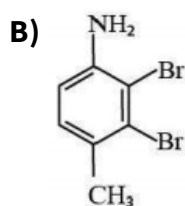
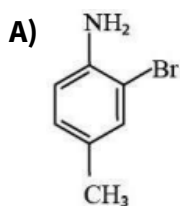
D) X



Y



6. Q.Id: 155306
4-Nitro toluene(para-nitro toluene) on reduction with Fe/HCl and then electrophilic bromination with an excess amount of Br₂ gives



7. Q.Id: 155305
The number of six and five membered rings present in norethindrone (a synthetic progesterone) are respectively

A) 2 and 2

B) 3 and 1

C) 3 and 3

D) 3 and 2

8. Q.Id: 155304
Which of the following are reducing sugars?

I) Sucrose

II) Ribose

III) Lactose

IV) Fructose

A) I, II only

B) II, III, IV Only

C) II, III only

D) I, II, IV only

9. Q.Id: 155303
Type of reaction involved in the initial step in the formation of Bakelite

A) Electrophilic substitution

B) Electrophilic addition

C) Nucleophilic substitution

D) Nucleophilic addition

10. Q.Id: 155302
Coordination number of Fe in the complexes
[Fe(CN)₆]⁴⁻, [Fe(CN)₆]³⁻ and [FeCl₄]⁻ would be respectively

A) 2,3,3

B) 6,6,4

C) 6,3,3

D) 6,4,6

17. Q.Id: 155295
What is the standard cell potential for the reaction $K=1$ (equilibrium constant)
- A) One
B) Zero
C) 2.303
D) Infinity
18. Q.Id: 155294
The vapour pressure of pure water is 23 mm Hg. The vapour pressure of an aqueous solution which contains 10 mass percent of solute 'A' having molecular weight 50 is
- A) 0.003 atm
B) 34.5 atm
C) 22 atm
D) 0.028 atm
19. Q.Id: 155293
15% aqueous solution of glucose (molecular weight = 180 g/mol) is isotonic with 8% aqueous solution containing an unknown non-dissociable solute. What is the molecular weight of the unknown solute?
- A) 108
B) 96
C) 84
D) 9.6
20. Q.Id: 155292
The angle between (100) and (110) planes of FCC lattice is
- A) 90°
B) 0°
C) 45°
D) 120°
21. Q.Id: 155291
The correct order of reactivity of hydrogen halides with propene is
- A) $\text{HCl} > \text{HBr} > \text{HI}$
B) $\text{HBr} > \text{HI} > \text{HCl}$
C) $\text{HI} > \text{HBr} > \text{HCl}$
D) $\text{HCl} > \text{HI} > \text{HBr}$
22. Q.Id: 155290
Which of the following sets of functional groups is meta-directing group?
- A) $-\text{NO}_2, -\text{NH}_2, -\text{COOH}, -\text{COOR}$
B) $-\text{NO}_2, -\text{CHO}, -\text{SO}_3\text{H}, -\text{COR}$
C) $-\text{CN}, -\text{CHO}, -\text{NHCOCH}_3, -\text{COOR}$
D) $-\text{CN}, -\text{NH}_2, -\text{NHR}, -\text{OCH}_3$

23. Q.Id: 155289
The correct order of the relative stability of the following carbanions is
(i) $\text{HC}\equiv\text{C}^-$ (ii) $\text{CH}_2=\text{CH}-\text{CH}_2^-$ (iii) $\text{H}_2\text{C}=\text{CH}^-$ (iv) $(\text{C}_6\text{H}_5)_2\text{CH}^-$
- A) (i) > (iv) > (ii) > (iii) B) (iii) > (iv) > (i) > (ii)
C) (iv) > (ii) > (i) > (iii) D) (iv) > (i) > (ii) > (iii)
24. Q.Id: 155288
Which of the following molecules is present in photochemical smog?
- A) SO_2 B) NO_2
C) CO_2 D) CO
25. Q.Id: 155287
When graphite is heated at 300°C with potassium vapour, it forms C_8K compound that shows one of the following property.
- A) Conducting and diamagnetic B) Non-conducting and diamagnetic
C) Conducting and paramagnetic D) Non-conducting and paramagnetic
26. Q.Id: 155286
When orthoboric acid (H_3BO_3) is subjected to strong heating, the residue left is
- A) Diborane B) Boron
C) Boric anhydride D) Borax
27. Q.Id: 155285
What is the increasing order of hydration enthalpies of alkali metal ions ?
- A) $\text{Rb}^+ < \text{Cs}^+ < \text{K}^+ < \text{Na}^+ < \text{Li}^+$ B) $\text{Cs}^+ < \text{Rb}^+ < \text{K}^+ < \text{Li}^+ < \text{Na}^+$
C) $\text{Cs}^+ < \text{Rb}^+ < \text{K}^+ < \text{Na}^+ < \text{Li}^+$ D) $\text{Cs}^+ < \text{Rb}^+ < \text{Na}^+ < \text{K}^+ < \text{Li}^+$
28. Q.Id: 155284
What will be the organic compound formed when, aluminium carbide react with deuterated water?
- A) CD_3OD B) DCOOD
C) CD_4 D) $\text{D}_3\text{C}-\text{O}-\text{CD}_3$

34. Q.Id: 155278
A vessel of volume 24.6 L contains 1.5 moles of H_2 and 2.5 moles of N_2 , at 300 K. Calculate the partial pressure of N_2 in the vessel.

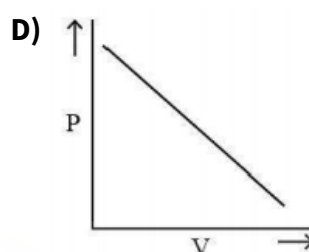
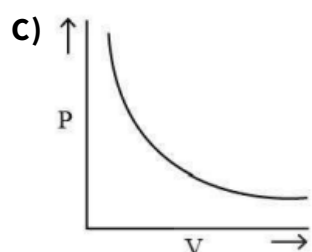
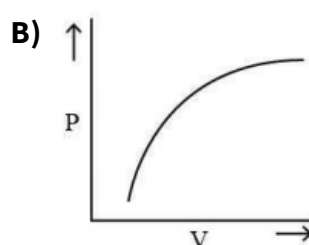
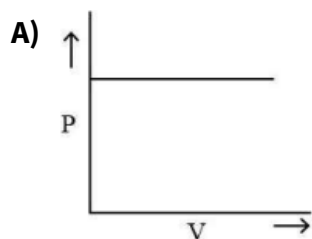
A) 1.5 atm

B) 2.0 atm

C) 2.5 atm

D) 3.0 atm

35. Q.Id: 155277
Which among the following graphs, correctly represents the Boyle's Law?



36. Q.Id: 155276
Find out the correct hybridization of the central atom in BCl_3 , PCl_5 , NH_3 and SF_6

A) $(BCl_3:sp^3); (PCl_5:sp^3d^2); (NH_3:sp^2)$ and $(SF_6:sp^3d)$

B) $(BCl_3:sp^2); (PCl_5:sp^3d); (NH_3:sp^3)$ and $(SF_6:sp^3d^2)$

C) $(BCl_3:sp^2); (PCl_5:sp^3d^2); (NH_3:sp^3)$ and $(SF_6:sp^3d)$

D) $(BCl_3:sp^3); (PCl_5:sp^3d^2); (NH_3:sp^2)$ and $(SF_6:sp^3d^2)$

37. Q.Id: 155275
The correct order of H — N — H bond angles of ammonia, ammonium and amide are

A) $NH_2^- > NH_3 > NH_4^+$

B) $NH_4^+ > NH_3 > NH_2^-$

C) $NH_3 > NH_2^- > NH_4^+$

D) $NH_3 > NH_4^+ > NH_2^-$

38. Q.Id: 155274
 Among the following, the pair of elements having same electronegativity values are
 (i) H and P
 (ii) Be and Al
 (iii) N and Cl
 (iv) C and P
- A) (i),(ii) and (iii) only B) (i),(iii) and (iv) only
 C) (ii),(iii) and (iv) only D) (i),(ii) (iii) and (iv)

39. Q.Id: 155273
 Find the correct set with iso electronic species ?

- A) $N^{3-}, F^-, O_2, Ca^{2+}$ B) $Ca^{2+}, Cl^-, Al^{3+}, O_2^-$
 C) $N^{3-}, Mg^{2+}, F^-, O^{2-}$ D) $Mg^{2+}, O_2^-, Cl^-, N_3^-$

40. Q.Id: 155272
 The correct order of decreasing energy for the electrons whose quantum numbers, n and l are given below, is

- A) n = 5 and l = 2
 B) n = 5 and l = 0
 C) n = 4 and l = 3
 D) n = 4 and l = 1

- A) A>C>B>D B) A>B>C>D
 C) C>A>D>B D) A>B>D>C

41. Q.Id: 155271
 In the two elements ${}_{Z_1}A^{M_1}$ and ${}_{Z_2}B^{M_2}$, the following relations are true.
 $M_1 \neq M_2$ and $Z_1 \neq Z_2$ but $M_1 - Z_1 = M_2 - Z_2$. These elements are (M is atomic weight, Z is atomic number)

- A) Isotonic B) Isobaric
 C) Isotopic D) Isoelectronic

42. Q.Id: 155270

A message signal is super-imposed with a carrier signal. The resulting modulating signal $C_m(t)$ is given by $C_m(t) = A_1 \sin(\omega_1 t) + A_2 \sin(\omega_2 t) - A_3 \sin(\omega_3 t)$ where $\omega_2 < \omega_1 < \omega_3$. The modulation index mid the angular frequency of the message signal respectively are

A) $\frac{A_2}{A_1}, \frac{\omega_3 - \omega_1}{2}$

B) $\frac{2A_2}{A_1}, \omega_3 - \omega_1$

C) $\frac{A_1}{2A_2}, \frac{\omega_3 - \omega_1}{2}$

D) $\frac{2A_2}{A_1}, \frac{\omega_3 - \omega_2}{2}$

43. Q.Id: 155269

In a Zener diode

A) Only p-region is heavily doped

B) Only n-region is heavily doped

C) Both p & n region are heavily doped

D) Both p & n region are lightly doped

44. Q.Id: 155268

A p-n junction diode can with stand upto 20 mA current under forward bias. The diode has a potential difference of 0.5V across it, which is assumed to be independent of current. What is the maximum voltage of the battery used to forward bias the diode when a resistance of 125Ω is connected in series with it?

A) 3.0 V

B) 2.5 V

C) 3.2 V

D) 2.0 V

45. Q.Id: 155267

A radioactive element which can decay by two processes, has half-life t_1 for first process and half - life t_2 for second process. Let (t) be the effective average — life of this element. The correct statement is

A) $(t) < \frac{t_1 t_2}{t_1 + t_2}$

B) $(t) = \frac{t_1 t_2}{t_1 + t_2}$

C) $(t) > \frac{t_1 t_2}{t_1 + t_2}$

D) $(t) = \ln 2 \left(\frac{t_1 + t_2}{t_1 t_2} \right)$

46. Q.Id: 155266
 in the Bohr model an electron of mass m moves in a circular orbit around the proton. Considering the orbiting electron to be a circular current loop, the magnetic moment of the hydrogen atom, when the electron is in n^{th} excited state, is:
 (Assume h = Planck's constant)

- A) $\left(\frac{e}{2m} \frac{n^2 h}{2\pi}\right)$ B) $\left(\frac{e}{m}\right) \frac{nh}{2\pi}$
 C) $\left(\frac{e}{2m}\right) \frac{nh}{2\pi}$ D) $\left(\frac{e}{m}\right) \frac{n^2 h}{2\pi}$

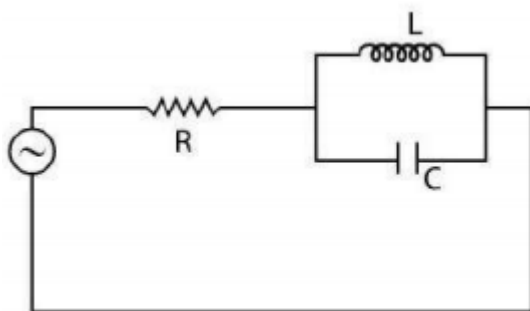
47. Q.Id: 155265
 When the energy of incident radiation is increased by 20 %, the kinetic energy of the photo electrons emitted from a metal surface increased from 0.5 eV to 0.8 eV. The work function of the metal is

- A) 0.65 eV B) 1.0 eV
 C) 1.3 eV D) 1.5 eV

48. Q.Id: 155264
 At an instant, a plane electromagnetic wave has its magnetic field in the direction of the vector $\hat{i} - \hat{j}$ and its electric field is in the direction of $\hat{i} + \hat{j}$. The wave is travelling along which direction?

- A) + x direction B) - x direction
 C) + z direction D) - z direction

49. Q.Id: 155263
 The LCR circuit shown below is driven by an ideal AC voltage source.



At frequency $f = \frac{1}{2\pi\sqrt{LC}}$, the correct statement is

- A) The current through R is zero B) The current through R is infinite
 C) The current through R depends on the value of L and C D) The current through R depends on the value of R and not L and C

50. Q.Id: 155262
A circular coil consists 70 closely wound turns and has a radius of 10 cm. An externally produced magnetic field of magnitude 2×10^{-3} T is applied perpendicular to the coil. The net flux through the coil is found to vanish when the current in the coil is 2.2 A. The inductance of the coil is

A) 2 mH

B) 3 mH

C) 4 mH

D) 1.5 mH

51. Q.Id: 155261
Let m and r are the dipole moment and radius of earth respectively. Then the earth's magnetic field at the equator is

A) $\frac{\mu_0 m}{4\pi r^3}$

B) $\frac{\mu_0 m}{8\pi r^3}$

C) $\frac{\mu_0 m}{2\pi r^3}$

D) $\frac{\mu_0 m}{\pi r^3}$

52. Q.Id: 155260
A coil having 100 turns is wound tightly in the form of a spiral with inner and outer radii 1 cm and 2 cm respectively. When a current 1A passes through the coil, the magnetic field at the centre of the coil is

A) $2\pi \ell n(2)$ mT

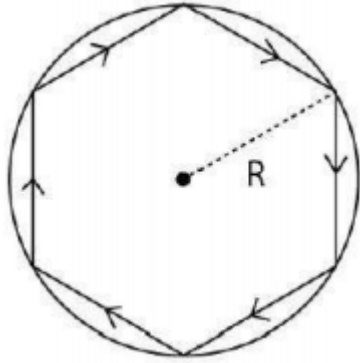
B) $\frac{\pi}{2} \ell n(2)$ mT

C) $\pi \ell n(2)$ mT

D) $\sqrt{2} \pi \ell n(2)$ mT

53. Q.Id: 155256

A conducting wire is in the shape of a regular hexagon which is inscribed inside an imaginary circle of radius R . If a current I flows the wire. the magnitude of magnetic field at the centre of the circle is



A) $\frac{\mu_2 J}{2\sqrt{3}\pi R}$

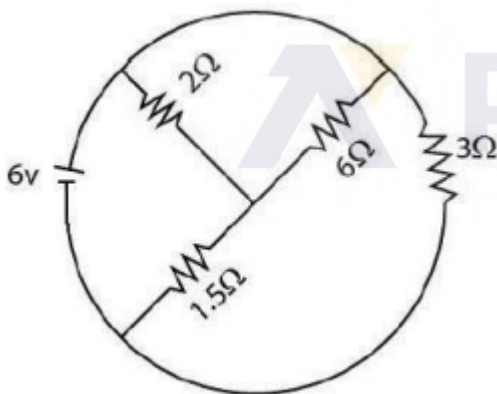
B) $\frac{\sqrt{3}\mu_2 J}{2\pi R}$

C) $\frac{3\mu_0 J}{2\pi R}$

D) $\frac{\sqrt{3}\mu_0 J}{\pi R}$

54. Q.Id: 155252

The total current supplied to the following circuit by the battery is



A) 4 A

B) 2 A

C) 1 A

D) 6 A

55. Q.Id: 155251

A conducting wire of cross-sectional area 1 cm^2 has 3×10^{23} charge carriers per m^3 . If wire carries a current of 24 mA, then drift velocity of carriers is

A) $5 \times 10^{-2} \text{ m/s}$

B) 0.5 m/s

C) $5 \times 10^{-3} \text{ m/s}$

D) $5 \times 10^{-6} \text{ m/s}$

56. Q.Id: 155249

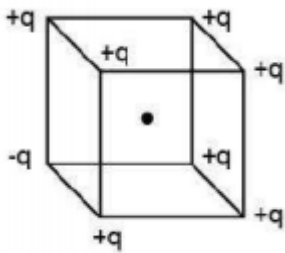
A capacitor is fully charged with a battery and then disconnected. A dielectric is then inserted into the capacitor. How do charges on surface of the dielectric and outer surface of the plates of the capacitor would change respectively?

- A) increases, decreases
B) decreases, increases
C) increases, remain unchanged
D) remains unchanged, increases

57. Q.Id: 155246

A cube of side L has point charges $+q$ located at its seven vertices and $-q$ at remaining one vertex. The electric field at its center is found to be

$|\vec{E}| = \alpha \left(\frac{q}{4\pi \epsilon_0 L^2} \right)$. The magnitude of constant α is



- A) $\frac{4}{3}$
B) $\frac{8}{3}$
C) 3
D) 1

58. Q.Id: 155244

The shape of wavefront of light diverging from point source

- A) spherical
B) planar
C) cylindrical
D) circular

59. Q.Id: 155243

What minimum separation between two objects a human eye would be able to resolve, if the eye pupil diameter is 2mm, and the two objects are 20m away from the eye.

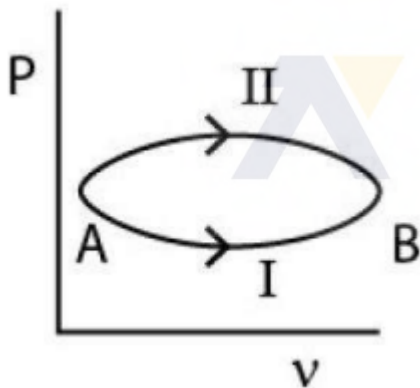
(Assume human eye to be equivalent to a convex lens and consider the average wave length of light as 600nm)

- A) 7.32 mm
B) 8.72 mm
C) 6.2 mm
D) 4.71 mm

60. Q.Id: 155242
 The magnifications produced by a convex lens for two position of an object are 4 and 3 respectively. If the distance of separation between the two positions of the object is 2 cm, then the focal length of the lens is
- A) 20 cm B) 16 cm
 C) 28 cm D) 24 cm

61. Q.Id: 155240
 An organ pipe with both ends open has a length $L = 25$ cm. An extra hole is created at position $\frac{L}{2}$. The lowest frequency of sound produced is (Assume speed of sound = 340 m/s)
- A) 680 Hz B) 340 Hz
 C) 1360 Hz D) 4352 Hz

62. Q.Id: 155237
 A system goes from A to B via two processes I and II as shown in figure. If ΔU_1 and ΔU_2 are the changes in internal energies in the processes I and II respectively, then the relation between ΔU_1 and ΔU_2 is



- A) $\Delta U_1 = \Delta U_2$ B) $\Delta U_2 < \Delta U_1$
 C) $\Delta U_2 > \Delta U_1$ D) Undetermined
63. Q.Id: 155235
 A carnot engine whose efficiency is 40%, receives heat at at 500 K. If the efficiency is to be 50%, the source temperature for the same exhaust temperature is
- A) 900 K B) 600 K
 C) 700 K D) 800 K

64. Q.Id: 155233
An ideal gas at temperature T , pressure P occupies a volume V . If its temperature is halved and pressure doubled, what is its new volume?

A) $\frac{V}{4}$

B) $\frac{V}{2}$

C) V

D) $2V$

65. Q.Id: 155232
A heating element of mass 100 g and having specific heat of $1 \text{ J/(g}^\circ\text{C)}$ is exposed to surrounding air at 27°C . The element attains a steady state temperature of 127°C while absorbing 100 W of electric power. If the power is switched off. then approximate time taken by the element to cool down to 126°C will be
(Neglect radiation)

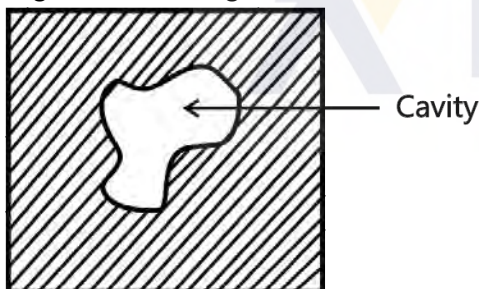
A) 0.1 s

B) 1.0 s

C) 5.0 s

D) 10.0 s

66. Q.Id: 155231
A block of iron contains a hollow cavity as shown below. The block weighs 6000 N in air and 4000 N in water. If the density of iron and water are 6 g/cm^3 and 1 g/cm^3 , then the volume of the cavity is (Assume $g = 10 \text{ m/s}^2$)



(Assume $g = 10 \text{ m/s}^2$)

A) 0.05 m^3

B) 0.5 m^3

C) 0.25 m^3

D) 0.1 m^3

67. Q.Id: 155228
A steel rod has a radius of 10 mm and a length of 1 m. A 80 kN force stretches it along its length. If the Young's modulus of the rod is $2 \times 10^{11} \text{ N/m}^2$, then the change in length is

A) $\frac{2}{\pi} \text{ mm}$

B) $\frac{4}{\pi} \text{ mm}$

C) $\frac{3}{\pi} \text{ mm}$

D) 1 mm

68. Q.Id: 155227
 A planet is moving in an elliptical orbit round the sun. The work done on the planet by the gravitational force of the sun:
- is zero in no part of the motion
 - is zero in some parts of the motion
 - is zero in one complete revolution
 - is zero in any small part of the orbit
- A) Only (c) is true B) Only (b),(c),(d) are true
 C) Only (b) and (c) are true D) Only (a) is true
69. Q.Id: 155209
 Consider a single harmonic motion (SHM). Let K and U be kinetic energy and potential energy when the displacement in SHM is one-half $\left(\frac{1}{2}\right)$ the amplitude. The correct statement is
- $\frac{K}{U} = 1$
 - $\frac{K}{U} = \frac{1}{2}$
 - $\frac{K}{U} = \frac{4}{3}$
 - $\frac{K}{U} = 3$
70. Q.Id: 155205
 A rod of length L revolves in a horizontal plane about the axis passing through its center and perpendicular to its length. The angular velocity of the rod is ω . If A is the area of cross-section of the rod and ρ is its density, then the rotational kinetic energy of the rod is
- $\frac{1}{3}AL^3\rho\omega$
 - $\frac{1}{2}AL^3\rho\omega^2$
 - $\frac{1}{24}AL^3\rho\omega^2$
 - $\frac{1}{18}AL^3\rho\omega^2$
71. Q.Id: 155204
 A solid sphere of mass 2 kg rolls on a smooth horizontal surface at 10 m/s. It then rolls up a smooth inclined plane of inclination 30° with the horizontal. The height attained by the sphere before it stop is [Take g as 10 m/sec^2]
- 70 cm
 - 701 cm
 - 7.0 m
 - 70 m

72. Q.Id: 155203

An elevator of mass 500 kg is ascending upwards with a constant acceleration $a = 2 \text{ m/s}^2$. What is the work done by the tension in the elevator cable during its climb by 12 m?

(Take $g = 10 \text{ m/s}^2$)

A) 36 KJ

B) 48 KJ

C) 72 KJ

D) 100 KJ

73. Q.Id: 155202

A force of 4 N acts on a 10 Kg body initially at rest. Let W_1 is work done by force during $0 \leq t \leq 1\text{s}$. Likewise W_2 is the work done by force during $1 \leq t \leq 2\text{s}$, where t is

time. The ratio $\frac{W_2}{W_1}$ is

A) 1

B) 2

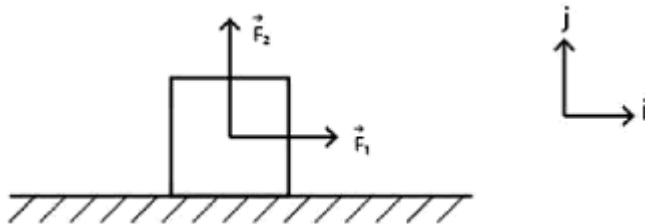
C) $\frac{1}{2}$

D) 3

74. Q.Id: 155201

A block of mass $m = 2 \text{ Kg}$ is initially at rest on a horizontal surface. A horizontal force $\vec{F} = (6\text{N}) \hat{i}$ and a vertical force $\vec{F}_2 = (10\text{N}) \hat{j}$ are then applied to the block. The coefficients of static friction and kinetic friction for the block and the surface are 0.4 and 0.25 respectively. The magnitude of the frictions force acting on the block is

(Assume $g = 10 \text{ m/s}^2$)



A) 2.5 N

B) 4.0 N

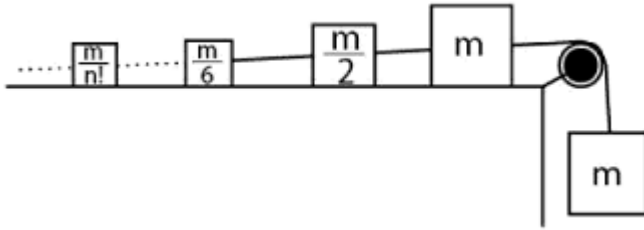
C) 3.3 N

D) 3.0 N

75. Q.Id: 155200

An infinite number of masses are placed on a frictionless table and they are connected via mass less strings. Their masses follow the sequence.

$m, \frac{m}{2}, \frac{m}{6}, \dots, \frac{m}{n!}, \dots$ and they are further connected to a mass m that hangs over a massless pulley. The acceleration of the hanging mass is



A) $\frac{g}{e-1}$

B) $\frac{g}{e+1}$

C) $\frac{g}{e}$

D) $\frac{g}{2e}$

76. Q.Id: 155199

A river 200 m wide is flowing at a rate of 3.0 m/s. A boat is sailing at a velocity of 15 m/s with respect to the water in a direction perpendicular to the river. How far from the point directly opposite to the starting point does the boat reach on the opposite bank?

A) 25 m

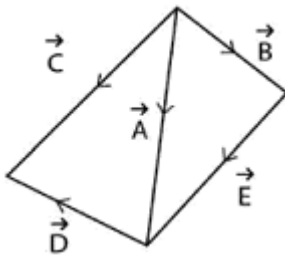
B) 60 m

C) 40 m

D) 50 m

77. Q.Id: 155198

Consider following vectors



The correct statement is

A) $\vec{E} = \vec{A} - \vec{B}$ and $\vec{A} = \vec{D} + \vec{C}$

B) $-\vec{E} = -\vec{A} + \vec{B}$ and $\vec{A} = -\vec{D} + \vec{C}$

C) $\vec{E} = -\vec{A} - \vec{B}$ and $\vec{E} = -\vec{B} + \vec{D} + \vec{C}$

D) $\vec{E} = -\vec{A} - \vec{B}$ and $\vec{E} = -\vec{B} + \vec{C} + \vec{D}$

78. Q.Id: 155197

A particle moving along x-axis has acceleration f . at time t . given by

$f = f_0 \left(1 - \frac{t}{T}\right)$, Where f_0 and T are constants. The particle at $t = 0$ has zero velocity. In the time interval between $t = 0$ and the instant when $f = 0$, the particle's velocity is

A) $\frac{1}{2}f_0T^2$

B) f_0T^2

C) $\frac{1}{2}f_0T$

D) f_0T

79. Q.Id: 155196

A person moves 30 m north and then 20 m towards east and finally $30\sqrt{2}$ m in south west direction. The displacement of the person from the origin will be

A) 10 m along north

B) 10 m along south

C) 10 m along west

D) Zero

80. Q.Id: 155195

What is the dimension of $\frac{1}{\mu_0\epsilon_0}$?

(μ_0 = magnetic permeability

ϵ_0 = permittivity of free space)

A) L^2T^{-2}

B) LT^{-1}

C) L^2T^2

D) LT^2

81. Q.Id: 155194

Let G, W, E and S be relative strength of gravitational, weak-nuclear electromagnetic and strong-nuclear forces respectively. The correct statement is

A) $S > W > E > G$

B) $E > W > S > G$

C) $S > E > W > G$

D) $S > E > G > W$

82. Q.Id: 155193

The general solution of the differential equation $(1 + y^2)dx = (\tan^{-1}y - x)dy$ is

A) $x = (\tan^{-1}y) - 1 + C e^{-\tan^{-1}y}$

B) $x = (\tan^{-1}y) - 1 + C e^{\tan^{-1}y}$

C) $x = (\tan^{-1}y) - 1 + C$

D) $x = (\tan^{-1}y) + C e^{-\tan^{-1}y}$

83. Q.Id: 155192

The general solution of the differential equation

$(x - 2y + 1)dy - (3x - 6y + 2)dx - 0$ is

A) $\left| x + 2y + \frac{3}{5} \right|^{\frac{2}{25}} \cdot e^{115(x+2y)} = C$

B) $\left| x - 2y + \frac{3}{5} \right|^{\frac{2}{25}} \cdot e^{\frac{1}{5}(x+2y)} = C$

C) $\left| x - 2y + \frac{3}{5} \right|^{\frac{2}{25}} \cdot e^{\frac{1}{5}(6x+2y)} = C$

D) $\left| x - 2y + \frac{1}{5} \right|^{\frac{2}{25}} \cdot e^{\frac{1}{5}(x-2y)} = C$

84. Q.Id: 155191

The differential equation for which $lx^2 + my^2 = x + y$ is the general solution is

A) $\begin{vmatrix} x^2 & y^2 & x+y \\ 2x & 2y'y' & y'+1 \\ 2 & 2yy'' & y'' \end{vmatrix} = 0$

B) $\begin{vmatrix} x^2 & y^2 & x+y \\ 2x & 2yy' & 1+y' \\ 2 & 2(y^2+y'') & y'' \end{vmatrix} = 0$

C) $\begin{vmatrix} x^2 & y^2 & x+y \\ 2x & 2yy' & y+1 \\ 2 & 2(y'^2+y'y'') & y'' \end{vmatrix} = 0$

D) $\begin{vmatrix} x^2 & y^2 & x+y \\ 2x & 2y & 1+y' \\ 2 & 2yy'y'' & y'' \end{vmatrix} = 0$

85. Q.Id: 155190

The area (in sq. units) of the portion lying above the X-axis and enclosed between the curves $y^2 = 2ax - x^2$ and $y^2 = ax$ is

A) $a^2 \left(\frac{-\pi}{2} + \frac{2}{3} \right)$

B) $a^2 \left(\frac{2}{3} + \frac{\pi}{4} \right)$

C) $a^2 \left(\frac{\pi}{4} - \frac{2}{3} \right)$

D) $a^2 \left(\frac{\pi}{4} + \frac{2}{3} \right)$

86. Q.Id: 155189

$\int_3^5 (x-3)^3(5-x)^5 dx =$

A) $\frac{64}{63}$

B) $\frac{25}{7}$

C) $\frac{3}{32}$

D) $\frac{16}{25}$

87. Q.Id: 155188

If $f(x) = \sin^6 x + \cos^6 x + 2\sin^3 x \cos^3 x$, then $\int_0^{\pi/4} \frac{\sin^2 2x}{f(x)} dx =$

A) 2

B) $\frac{2}{3}$

C) $-\frac{2}{3}$

D) $\frac{1}{6}$

88. Q.Id: 155187

The positive integer $n \leq 5$ for which $\int_0^1 e^x(x-1)^n dx = 16 - 6e$ is

A) 5

B) 4

C) 3

D) 2

89. Q.Id: 155186

$I_{m,n} = \int x^m (\log x)^n dx =$

A) $\frac{x^{m+1}}{m+1} (\log x)^n - \frac{n}{m+1} I_{m,n-1}$

B) $\frac{x^m}{m} (\log x)^n - \frac{n-1}{m+1} I_{m+1,n-1}$

C) $\frac{x^{m+1}}{m} \frac{(\log x)^{n+1}}{n+1} - \frac{n}{m+1} I_{m,n-1}$

D) $x^m \frac{(\log x)^{n+1}}{n+1} - \frac{n}{m+1} I_{m,n-1}$

90. Q.Id: 155185

$\int \frac{25x^2 + 8}{25x^2 + 9} dx =$

A) $\frac{x}{2} \sqrt{25x^2 + 9} + \frac{11}{10} \sinh^{-1} \left(\frac{5x}{3} \right) + C$

B) $\frac{x}{2} \sqrt{25x^2 + 9} - \frac{7}{10} \log \left(\frac{5x + \sqrt{25x^2 + 9}}{3} \right) + C$

C) $\frac{x}{2} \sqrt{25x^2 + 9} + \frac{7}{10} \sinh^{-1} \left(\frac{5x}{3} \right) + C$

D) $\frac{x}{2} \sqrt{25x^2 + 9} + \frac{11}{10} \log \left(\frac{5x - \sqrt{25x^2 + 9}}{3} \right) + C$

91. Q.Id: 155184

If $\int e^{\sin^2 x} (\sin x \cos x + \cos^3 x \sin x) dx = e^{\sin^2 x} (1 + f(x)) + c$. then $f'(x) =$

A) $\frac{1}{2} \sin^2 x$

B) $\frac{1}{2} \cos^2 x$

C) $-\frac{1}{2} \cos 2x$

D) $-\frac{1}{2} \sin 2x$

92. Q.Id: 155183
A function $y = f(x)$ with $f(-1) = -249$ has no maximum and has only one minimum at $x = 5$ with $f(5) = 75$. Which one of the following is true?

- A)** At some point in $(-1, 5)$, $f(x)$ is discontinuous
B) The minimum value cannot be 75 since $f(-1) < f(5) = 75$
C) $f(x)$ is discontinuous at every point of \mathbb{R}
D) $f(x)$ is discontinuous on \mathbb{R}

93. Q.Id: 155182

Statement (I): If $a_0 + \frac{a_1}{2} + \frac{a_2}{3} + \dots + \frac{a_n}{n+1} = 0$, where a_0, a_1, \dots, a_n are real numbers, then the polynomial $a_0 + a_1x + a_2x^2 + \dots + a_nx^n$ has a zero in the interval $(0,1)$

Statement (II): If $f: [a,b] \rightarrow \mathbb{R}$ is continuous on $[a,b]$ and f is differentiable in (a,b) , where $a > 0$ and if $\frac{f(a)}{a} = \frac{f(b)}{b}$, then there exists $c \in (a,b)$ such that $c f'(c) = f(c)$

- A)** Only (I) is true
B) Only (II) is true
C) Neither (I) nor (II) is true
D) Both (I) and (II) are true

94. Q.Id: 155181

$x_1, x_2 \in \mathbb{N}$. **if a line having slope 2 is a tangent to the curve $y = x^4 - 6x^3 + 13x^2 - 10x + 5$ at points $P(x_1, y_1)$ and $Q(x_2, y_2)$, then $x_1x_2 + y_1y_2 =$**

- A)** 7
B) -5
C) 13
D) -10

95. Q.Id: 155180

If the tangent and normal drawn to the curve

$x = a(\theta + \sin \theta), y = a(1 - \cos \theta)$ at $P\left(\theta = \frac{\pi}{2}\right)$ **cuts the X-axis at A and B respectively, then the area (in sq. units) of ΔPAB is**

- A)** $\frac{a^2}{\sqrt{2}}$
B) $\frac{\sqrt{2}}{a^2}$
C) a^2
D) $2a^2$

96. Q.Id: 155179

If $2^x + 2^y = 2^{x+y}$, then $\frac{dy}{dx} =$

- A)** $1 - 2^y$
B) $1 - 2^{-y}$
C) $1 + 2^y$
D) $1 + 2^{-y}$

102. Q.Id: 155163

If the direction ratios a, b, c of a line L satisfy the relations $ab + bc + ca = 0$ and $6ab + 9bc + 8c^2 = 0$, then the direction cosines of the line L are

A) $\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}$

B) $\frac{2}{\sqrt{7}}, \frac{1}{\sqrt{7}}, \frac{-2}{\sqrt{7}}$

C) $\frac{-1}{\sqrt{6}}, \frac{\sqrt{3}}{\sqrt{6}}, \frac{\sqrt{2}}{\sqrt{6}}$

D) $\frac{-3}{7}, \frac{2}{7}, \frac{-6}{7}$

103. Q.Id: 155155

$E(1, 0, 0), F(0, 2, 0), G(0, 0, 3)$ are respectively the mid points of the sides AB, BC, CA of $\triangle ABC$. If a_1, b_1, c_1 and a_2, b_2, c_2 are respectively the direction ratios

of AF and BG , then $\frac{a_1^2 + b_1^2 + c_1^2}{a_2^2 + b_2^2 + c_2^2} =$

A) $\frac{26}{41}$

B) $\frac{13}{26}$

C) $\frac{17}{43}$

D) $\frac{13}{43}$

104. Q.Id: 155146

A rectangular hyperbola passing through $(3, 2)$ has its asymptotes parallel to the coordinate axes. If $(1, 1)$ is the point of intersection of the two perpendicular tangents of that hyperbola, then its equation is

A) $xy = x + \frac{1}{y}$

B) $x\left(y + 1 + \frac{1}{x}\right) = 1$

C) $x(1 - y) = y - 1$

D) $xy = x + y + 1$

105. Q.Id: 155141

The equation of the ellipse with directrix $3x + 4y - 5 = 0$, focus $(1, 2)$ and eccentricity $\frac{1}{2}$, is

A) $x^2 + 84y^2 - 24xy - 360y + 170x + 475 = 0$

B) $91x^2 + 84y^2 - 24xy - 170x - 360y + 475 = 0$

C) $91x^2 + 84y^2 - 24xy - 170x + 360y + 475 = 0$

D) $91x^2 + 84y^2 - 24xy - 170x - 360y - 475 = 0$

106. Q.Id: 155136
If the sum of the distances from the foci to the centre $O(0, 0)$ of an ellipse is $8\sqrt{6}$ units and the area of the smallest rectangle in which that ellipse is inscribed is 80 sq. units, then the equation of such an ellipse is
- A) $\frac{x^2}{100} + \frac{y^2}{64} = 1$ B) $\frac{x^2}{100} + \frac{y^2}{16} = 1$
C) $\frac{x^2}{10} + \frac{y^2}{4} = 1$ D) $\frac{x^2}{100} + \frac{y^2}{4} = 1$
107. Q.Id: 155132
If the tangent drawn at the point $P(4, 8)$ to the parabola $y^2 = 16x$ meets the parabola $y^2 = 16x + 80$ at A and B, then the midpoint of AB is
- A) (9,6) B) (4,8)
C) (4,1) D) (2,3)
108. Q.Id: 155128
If a circle with its centre at the focus of the parabola $y^2 = 2px$ is such that it touches the directrix of the parabola, then a point of intersection of the circle and the parabola is
- A) $\left(\frac{p}{2}, 2p\right)$ B) $\left(\frac{-p}{2}, p\right)$
C) $\left(\frac{p}{2}, -p\right)$ D) $\left(\frac{-p}{2}, -p\right)$
109. Q.Id: 155121
The centre of the circle passing through the points of intersection of the circles $(x+3)^2 + (y+2)^2 = 25$ and $(x-2)^2 + (y-3)^2 = 25$ and cutting the circle $(x+1)^2 + (y-2)^2 = 16$ orthogonally is
- A) $\left(\frac{-27}{2}, \frac{-25}{2}\right)$ B) (0,0)
C) $\left(\frac{16}{3}, \frac{-25}{4}\right)$ D) $\left(\frac{4}{7}, \frac{3}{7}\right)$
110. Q.Id: 155115
If the circles $x^2 + y^2 - 2x - 2y + k = 0$ and $x^2 + y^2 + 4x + 6y + 4 = 0$ touch each other externally, then the point of contact of the two circles is
- A) $\left(\frac{-1}{5}, \frac{-3}{5}\right)$ B) $\left(\frac{-1}{3}, \frac{-1}{3}\right)$
C) (-1,-3) D) (-1,-1)

111. Q.Id: 155109
If a circle of radius r touches the positive coordinate axes and also the circle $x^2 + y^2 - 12x - 10y + 52 = 0$ externally, then the distance between the centres of the two circles is
- A) 7 B) 5
C) 6 D) 8
112. Q.Id: 155106
If the circle $x^2 + y^2 - 4x + 6y + 13 - a^2 = 0$ and $x^2 + y^2 - 10x - 2y + 17 = 0$ intersect in two distinct points, then 'a' is
- A) $-8 < a < -2$ B) $a > 8$
C) $2 < a < -6$ D) $a < -8$
113. Q.Id: 155101
If the poles of the line $x - y = 0$ with respect to the circles $x^2 + y^2 - 2g_i x + c_i^2 = 0 (i = 1, 2, 3)$ are (α_i, β_i) then $\sum_{i=1}^3 \frac{\alpha_i + \beta_i}{g_i} =$
- A) 3 B) 6
C) $\frac{3}{2}$ D) $\frac{3}{4}$
114. Q.Id: 155096
Let P be the point of intersection of the lines $L_1 \equiv x - y - 7 = 0$ and $L_2 \equiv x + y - 5 = 0$. A (x_1, y_1) and B (x_2, y_2) are points on the lines $L_1 = 0$ and $L_2 = 0$ respectively such that $PA = 3\sqrt{2}$, $PB = \sqrt{2}$, $x_1 y_1 \geq 0$, $x_2 y_2 \geq 0$, then the angle made by the line segment AB at the origin is
- A) $\frac{\pi}{4}$ B) $\frac{\pi}{2}$
C) $\cos^{-1}\left(\frac{3}{4}\right)$ D) $\cos^{-1}\left(\frac{9}{\sqrt{85}}\right)$
115. Q.Id: 155093
Suppose O(0,0) is the origin and the line $L = x + y - \lambda = 0$ meets the curve $x^2 + y^2 - 2x - 4y + 2 = 0$ at A and B. If $\angle AOB = 90^\circ$ then the distance between such lines $L = 0$ is
- A) $\frac{1}{\sqrt{2}}$ B) $\frac{3}{\sqrt{2}}$
C) $\sqrt{2}$ D) $\sqrt{2} + 1$

116. Q.Id: 155084

If two equal sides of an isosceles triangle are given by the equations $7x - y + 3 = 0$ and $x + y - 3 = 0$, then the equation of its third side passing through the point $(2, -5)$ is

A) $x - 3y = 17$

B) $3x - y = 11$

C) $7x + 2y = 4$

D) $3x + y = 11$

117. Q.Id: 155080

If the equation of the straight line passing through the point of intersection of $x + 2y - 19 = 0$, $x - 2y - 3 = 0$ and which is at a perpendicular distance of n units from the point $(-2, 4)$ is $5x + by + c = 0$, then a possible value of $5 + b + c$ is

A) -108

B) 10

C) 86

D) -14

118. Q.Id: 155069

If the straight line passing through the point $P(3, 4)$ makes an angle $\frac{\pi}{6}$ with the positive direction of X-axis and meets the line $12x + 5y + 10 = 0$ at Q , then the length of PQ is

A) $\frac{44}{12\sqrt{2} + 9}$

B) $\frac{66}{12\sqrt{3} + 5}$

C) $\frac{132}{12\sqrt{3} + 5}$

D) $\frac{148}{6\sqrt{2} + 3}$

119. Q.Id: 155065

Let C be a curve $ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$ in a cartesian plane. By

rotating the coordinate axes through an angle $\frac{\pi}{4}$ in the positive direction, if the transformed equation of C is $Y^2 + XY - X = 0$, then $(h^2 - ab) - 2gf =$

A) 0

B) 2

C) 1

D) -1

120. Q.Id: 155057

If $A = (1, 2)$, $B = (2, 1)$ and P is any point satisfying the condition $PA + PB = 3$, then the equation of the locus of P is

A) $16x^2 + 7y^2 - 64x - 48 = 0$

B) $x^2 + 10xy + 25y^2 - 34x - 170y = 0$

C) $32x^2 + 8xy + 32y^2 - 108x - 108y + 99 = 0$

D) $4x^2 + 12xy + 9y^2 - 20x - 30y = 0$

121. Q.Id: 155051
Let $X \sim B(n,p)$ with mean μ and variance σ^2 . If $\mu = 2$, $\sigma^2 = 3$, then $P(X \leq 3) =$

A) $\frac{15}{16}$

B) $\frac{2}{3}$

C) $\frac{14}{17}$

D) $\frac{1}{3}$

122. Q.Id: 155045
A target is to be destroyed in a bombing exercise and there is a 75% chance that a bomb will hit the target. Assuming that two direct hits are required to destroy the target completely, the minimum number of bombs to be dropped in order that the probability of destroying the target is not less than 99%, is

A) 4

B) 5

C) 6

D) 7

123. Q.Id: 155043
A number is selected at random from the set $\{1, 2, \dots, 100\}$. Given that the number selected is divisible by 2, the probability that it is also divisible by 3 or 5, is

A) $\frac{26}{50}$

B) $\frac{23}{50}$

C) $\frac{7}{50}$

D) $\frac{13}{50}$

124. Q.Id: 155038
Cards are drawn one after the other without replacement from a well-shuffled pack of cards until an ace card appears. If the probability that exactly 5 cards are drawn before the first ace card appears is $\frac{4}{49} \left(\frac{p_1 \cdot p_2 \cdot p_3}{p_4 \cdot p_5 \cdot p_6} \right)$, (p_i is prime, $i = 1, 2, 3, 4, 5, 6$) then $(\max\{p_i\} - \min\{p_i\}) =$

A) 12

B) 18

C) 20

D) 22

125. Q.Id: 155031
If the roots of each of the equations
 $2x^2 + x - 1 = 0$, $3x^2 - 10x + 3 = 0$ and $6x^2 + 11x - 2 = 0$ corresponds to probabilities
of three events of a random experiment, then those events are

- A)** Equally likely **B)** Exhaustive
C) Mutually exclusive **D)** Mutually independent

126. Q.Id: 155028
The mean deviation about the mean of the following data is nearly

Size(x)	1	3	5	7	9	11	13	15
Frequency(f)	3	3	4	14	7	4	3	4

- A)** 3.45 **B)** 3.25
C) 2.75 **D)** 2.95

127. Q.Id: 155027
The variance of the following frequency distribution is

Classes	0 - 10	10 - 20	20 - 30	30 - 40	40 - 50	50 - 60
Frequency	11	25	18	4	5	3

- A)** 165.3 **B)** 161.1
C) 282.1 **D)** 152.5

128. Q.Id: 155026

If \vec{b}, \vec{c} are non collinear vectors, $|\vec{c}| \neq 0$,
 $\vec{a} \times (\vec{b} \times \vec{c}) + (\vec{a} \cdot \vec{b})\vec{b} = (4 - 2\beta - \sin\alpha)\vec{b} + (\beta^2 - 1)\vec{c}$ **and** $(\vec{c} \cdot \vec{c})\vec{a} = \vec{c}$,

then the scalars α and β are

- A)** $\alpha = \frac{\pi}{2} + \frac{n\pi}{3}, n \in \mathbb{Z}; \beta = 1$ **B)** $\alpha = 2n\pi + \frac{\pi}{2}, n \in \mathbb{Z}$
C) $\alpha = \frac{\pi}{2} + (2n+1)\frac{\pi}{2}, n \in \mathbb{Z}; \beta = 2$ **D)** $\alpha = (2n+1)\frac{\pi}{2}, n \in \mathbb{Z}; \beta = \frac{3}{2}$

129. Q.Id: 155014

Let $\vec{p}, \vec{q}, \vec{r}$ be three non-coplanar vectors and

$$[\vec{p}, \vec{q}, \vec{r}] \vec{a} = \vec{q} \times \vec{r}, [\vec{p}, \vec{q}, \vec{r}] \vec{b} = \vec{r} \times \vec{p}, [\vec{p}, \vec{q}, \vec{r}] \vec{c} = \vec{p} \times \vec{q}. \text{ If } \vec{a}, \vec{b}, \vec{c}$$

denote the coterminous edges of a parallelepiped, then its height with the base having \vec{a} and \vec{b} is

A) $\frac{1}{|\vec{p}|}$

B) $\frac{1}{|\vec{a}|}$

C) $\frac{1}{|\vec{b}|}$

D) $\frac{1}{|\vec{q}|}$

130. Q.Id: 155003

Let $\vec{a} = \vec{i} + 2\vec{j} - 2\vec{k}$ and $\vec{b} = 2\vec{i} - \vec{j} - 2\vec{k}$. If the orthogonal projection vector of \vec{a} on \vec{b} be \vec{x} and the orthogonal projection vector of \vec{b} on \vec{a} be \vec{y} , then $|\vec{x} - \vec{y}| =$

A) $\frac{4}{9}\sqrt{26}$

B) $\frac{8}{9}\sqrt{10}$

C) $\frac{4}{9}\sqrt{10}$

D) $\frac{8}{9}\sqrt{26}$

131. Q.Id: 154999

$\vec{i}, \vec{m}, \vec{n}$ are three unit vectors in a right handed system and L is a line through the points A, B, C whose position vectors are

$\vec{p}\vec{i} + 7\vec{m} - 6\vec{n}$, $2\vec{i} + 5\vec{m} - 4\vec{n}$ and $\vec{i} + 4\vec{m} - 3\vec{n}$ respectively. If the equation of the plane containing L and the point $(-p, p, p + 1)$ is $ax + by + cz = 1$, then $p(a + b + c) =$

A) 0

B) $\frac{-40}{19}$

C) $\frac{40}{19}$

D) -6

132. Q.Id: 154991

If the point of intersection of the lines

$$\vec{r} = \vec{i} - 6\vec{j} + (p \sec \alpha)\vec{k} + t(\vec{i} + 2\vec{j} + \vec{k}) \text{ and } \vec{r} = 4\vec{j} + \vec{k} + \lambda(2\vec{i} + (p \text{ and } \alpha)\vec{j} + 2\vec{k}) \text{ is } 8\vec{i} + 8\vec{j} + 9\vec{k}, \left(\text{where } 0 < \alpha < \frac{\pi}{2}\right),$$

then $p =$

A) $\sqrt{5}$

B) $\sqrt{3}$

C) $\sqrt{2}$

D) 0

133. Q.Id: 154989
Match the following

List1

List2

$$\begin{aligned}\bar{a} &= 2\bar{i} + 3\bar{j} + 4\bar{k}, \\ \bar{b} &= 3\bar{i} + 4\bar{j} + 2\bar{k}, \\ \text{A. } \bar{c} &= 4\bar{i} + 2\bar{j} + 3\bar{k}\end{aligned}$$

$$\begin{aligned}\bar{a} &= \bar{i} + 2\bar{j} + 3\bar{k}, \\ \bar{b} &= 3\bar{i} + 4\bar{j} + 7\bar{k}, \\ \text{B. } \bar{c} &= -3\bar{i} - 2\bar{j} - 5\bar{k}\end{aligned}$$

$$\begin{aligned}\bar{a} &= 2\bar{i} - \bar{j} + \bar{k}, \\ \bar{b} &= \bar{i} - 3\bar{j} - 5\bar{k}, \\ \text{C. } \bar{c} &= -3\bar{i} - 4\bar{j} - 4\bar{k}\end{aligned}$$

$$\begin{aligned}\bar{a} &= \bar{i} + \bar{j} + \bar{k}, \\ \bar{b} &= \bar{i} + 2\bar{j} + 3\bar{k}, \\ \text{D. } \bar{c} &= 2\bar{i} - \bar{j} + \bar{k}\end{aligned}$$

E. .

A) A->i, B->iv, C->iii, D->ii

B) A->i, B->ii, C->iii, D->iv

C) A->v, B->i, C->iv, D->ii

D) A->v, B->i, C->iii, D->ii



134. Q.Id: 154966
In a ΔABC , with usual notation, if $r = r_1 - r_2 - r_3$, then $2R =$

A) a

B) b + c

C) c

D) c + a

135. Q.Id: 154964
The perimeter of a ΔABC is 6 times the arithmetic mean of the sine of its angles. If its side BC is of unit length, then $\angle A =$

A) $\frac{\pi}{6}$

B) $\frac{\pi}{3}$

C) $\frac{\pi}{2}$

D) π

136. Q.Id: 154959

If $\operatorname{Sech}^{-1}\left(\frac{1}{2}\right) - \operatorname{Cosech}^{-1}\left(\frac{3}{4}\right) = \log_e k$, then

A) $3k^2 - 12k - 1 = 0$

B) $3k^2 - 12k + 1 = 0$

C) $9k^2 - 12k + 1 = 0$

D) $9k^2 - 12k - 1 = 0$

137. Q.Id: 154956

The number of real roots of the equations $\sin[2\cos^{-1}\{\cot(2\tan^{-1}x)\}] = 0$ that are greater than or equal to one are

A) 1

B) 2

C) 3

D) 4

138. Q.Id: 154952

If $|\sin x - \cos^2 x| \geq |3 - 3\sin x + \sin^2 x| + 4|\sin x - 1|$ then $x =$

A) $(4n+1)\frac{\pi}{2}, n \in \mathbb{Z}$

B) $2n\pi + \frac{\pi}{3}, n \in \mathbb{Z}$

C) $n\pi + \frac{\pi}{2}, n \in \mathbb{Z}$

D) $2n\pi + \frac{\pi}{6}, n \in \mathbb{Z}$

139. Q.Id: 154948

If $A + B + C = 60^\circ$ then $\cos(30^\circ - A) + \cos(30^\circ - B) + \cos(30^\circ - C) + \sin(A + B + C) =$

A) $4\cos\frac{A}{2}\cos\frac{B}{2}\cos\frac{C}{2}$

B) $4\sin\frac{A}{2}\sin\frac{B}{2}\sin\frac{C}{2}$

C) $4\cos\frac{A}{2}\cos\frac{B}{2}\sin\frac{C}{2}$

D) $4\cos\frac{A}{2}\sin\frac{B}{2}\cos\frac{C}{2}$

140. Q.Id: 154942

If $\alpha = \frac{\sin^3 x}{\cos^2 x}$, $\beta = \frac{\cos^3 x}{\sin^2 x}$ and $\sin x + \cos x = k$ then $\alpha \sin x + \beta \cos x + 3 =$

A) $\frac{2}{(k^2-1)^2}$

B) $\frac{4}{(k^2-1)^2}$

C) $\frac{k^2-1}{2}$

D) $\frac{(k^2-1)^2}{4}$

141. Q.Id: 154938

The period of $\frac{\sin x}{\cos 3x} + \frac{\sin 3x}{\cos 9x} + \frac{\sin 9x}{\cos 27x} + \frac{\sin 27x}{\cos 81x}$ is

A) $\frac{2\pi}{3}$

B) $\frac{\pi}{81}$

C) 2π

D) π

142. Q.Id: 154935

If $\frac{1}{x^4+x^2+1} = \frac{Ax+B}{x^2+x+1} + \frac{Cx+D}{x^2-x+1}$, then $\cos^{-1}(A+B+C+D) =$

A) $\frac{\pi}{2}$

B) 0

C) $\frac{\pi}{6}$

D) $\frac{\pi}{3}$

143. Q.Id: 154932

For $z \in \mathbb{C}$, if $(1+z)^n = 1 + {}_n C_1 z + {}_n C_2 z^2 + \dots + {}_n C_n z^n$ and

$\sum_{r=0}^{100} {}_{100} C_r (\sin r x) = \left(2 \cos \frac{x}{2}\right)^{100} \sin k x$, then $k =$

A) 25

B) 100

C) 50

D) 75

144. Q.Id: 154930

Suppose l, m, n respectively represent the coefficient of x^{10} , the constant term and the coefficient of x^{-10} in the expansion of

$\left(ax^2 + \frac{b}{x^3}\right)^{15}$. If $\frac{l}{m} + \frac{m}{n} = \frac{26}{11}$, then $a^2 : b^2 =$

A) 16 : 9

B) 9 : 4

C) 4 : 1

D) 1 : 25

145. Q.Id: 154926

If 3 sisters and 8 other girls are together playing a game, then the number of ways in which all the girls are seated around a circle such that the three sisters are not seated together, is

A) $11! \times 8$

B) $8! \times 504$

C) $7! \times 210$

D) $8! \times 84$

146. Q.Id: 154922
The number of integers x, y, z, w satisfying $x + y + z + w = 25$ and $x, y, z \geq -1, w \geq 1$, is

A) ${}_{28}C_3$

B) ${}_{30}C_3$

C) ${}_{29}C_3$

D) ${}_{31}C_3$

147. Q.Id: 154919
If α, β, γ are the roots of the equation $x^3 + 3x^2 - x - 3 = 0$ then $(1 + \alpha^2)(1 + \beta^2)(1 + \gamma^2) =$

A) 16

B) 24

C) 36

D) 40

148. Q.Id: 154915
If the roots of $x^3 + ax^2 + bx + c = 0$ are in arithmetic progression with common difference 1, then

A) $9c = a(b - 2)$

B) $9c = a(2 - b)$

C) $9c - a^2(b - 2) = 0$

D) $9c - a^2(2 - b) = 0$

149. Q.Id: 154910
If the quadratic equations $3x^2 - 7x + 2 = 0$ and $kx^2 + 7x - 3 = 0$ have a common root then the positive value of k is

A) 6

B) $\frac{11}{4}$

C) 4

D) $\frac{7}{2}$

150. Q.Id: 154908

p and q are two roots of the equation $x^2 + 7x + 3 = 0$. If $\frac{3p}{1 - 2p}, \frac{3p}{1 - 2p}$ are the roots of $lx^2 + mx + n = 0$ and the greatest common divisor of l, m, n is 1, then $l - m + n =$

A) 11

B) -3

C) -1

D) 12

151. Q.Id: 154906

Let $A_r = \left(x + \frac{1}{x}\right)^3 \cdot \left(x^2 + \frac{1}{x^2}\right)^3 \cdot \left(x^3 + \frac{1}{x^3}\right)^3 \dots \left(x^r + \frac{1}{x^r}\right)^3$. If $x^2 + x + 1 = 0$, then $\frac{1}{A_3} + \frac{1}{A_6} + \frac{1}{A_9} + \frac{1}{A_{12}} + \dots \infty =$,

A) $\frac{1}{6}$

B) $\frac{2}{5}$

C) 1

D) $\frac{1}{7}$

152. Q.Id: 154902

For $n \in \mathbb{N}$, if $A_n = \cos\left(\frac{\pi}{2^n}\right) + i \sin\left(\frac{\pi}{2^n}\right)$, then $(A_1 A_2 A_3 A_4)^4 =$

A) $\frac{-1-i}{\sqrt{2}}$

B) 1

C) 0

D) $\frac{1-i}{\sqrt{2}}$

153. Q.Id: 154898

$A(z_1 = 2 + 2i)$, $B(z_2)$, $C(z_3)$ are three points on the Argand plane satisfying $|z_k - 2i| = 2$, ($k = 1, 2, 3$). If ΔABC encloses the maximum area, then the sum of the imaginary parts of z_2 and z_3 is

A) 1

B) 0

C) 4

D) -4

154. Q.Id: 154895

For some $a, b, c \in \mathbb{R}$, if $\sin 5\theta = a \cos^4\theta \sin\theta + b \cos^2\theta \sin^3\theta + c \sin^5\theta$, then $abc =$

A) -10

B) 10

C) 0

D) -50

155. Q.Id: 154890

$$\text{If } \begin{bmatrix} 2 & 1 & 1 \\ 0 & 3 & -1 \\ 1 & -1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix}, \text{ then } \begin{bmatrix} x \\ y \\ z \end{bmatrix} =$$

A) $\begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} + K \begin{bmatrix} 3 \\ 1 \\ -2 \end{bmatrix}, K \in \mathbb{R}$

B) $\begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} + K \begin{bmatrix} 1 \\ -2 \\ 3 \end{bmatrix}, K \in \mathbb{R}$

C) $\begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} + K \begin{bmatrix} -2 \\ 1 \\ 3 \end{bmatrix}, K \in \mathbb{R}$

D) $\begin{bmatrix} 1 \\ 0 \\ -1 \end{bmatrix} + K \begin{bmatrix} -2 \\ 1 \\ 3 \end{bmatrix}, K \in \mathbb{R}$

156. Q.Id: 154885

Let $[A]_{3 \times 3}$ be a non-singular matrix such that $A^{-1} = \frac{1}{3}(A^2 - 5A + 7I)$ then $17A^8 - 85A^7 + 119A^6 - 51A^5 - 19A^4 + 95A^3 - 133A^2 + 58A + I =$

A) 0

B) A

C) $A + I$

D) $A^2 + A + I$

157. Q.Id: 154881

A value of θ in $\left(0, \frac{\pi}{2}\right)$ and satisfying $\begin{vmatrix} 1 + \sin^2\theta & \cos^2\theta & 4 \sin 4\theta \\ \sin^2\theta & 1 + \cos^2\theta & 4 \sin 4\theta \\ \sin^2\theta & \cos^2\theta & 1 + 4 \sin 4\theta \end{vmatrix} = 0$ is

A) $\frac{\pi}{4}$

B) $\frac{\pi}{3}$

C) $\frac{5\pi}{24}$

D) $\frac{7\pi}{24}$

158. Q.Id: 154877

$n^5 - 5n^3 + 4n$ is divisible by 120 is true for

A) All positive integers n

B) All positive integers for $n \geq 3$ only

C) All positive integers for $n \geq 1$ only

D) All positive integers for $n \geq 5$ only

159. Q.Id: 154872

Let $[x]$ denote the greatest integer not more than x. If A and B are the

domains of the functions $f(x) = \frac{x - [x]}{\sqrt{|x| - x}}$ and $g(x) = \frac{x - [x]}{\sqrt{|x| + x}}$ respectively, then

A) $A \cup B = \mathbb{R}$

B) $A \cap B = \emptyset$

C) $A - B = (-\infty, 0)$

D) $B - A = (0, \infty)$

160. Q.Id: 154869

If $f: [-3, 2] \rightarrow [0, \sqrt[3]{x}]$ is an onto function defined by

$$f(n) = \begin{cases} 2 + \sqrt[3]{n}, & -3 \leq n \leq -1 \\ n^{2/3}, & -1 \leq n \leq 2 \end{cases} \text{ then } x =$$

A) 1

B) 2

C) 4

D) 6



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